# A Ka-Band Geophysical Model Function

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Abstract - A Ka-band geophysical model function is proposed. The model function is based on a similar previously-developed backscatter model, which showed a disadvantage at near crosswind azimuths for incidence angles of 47° to 50°. The new Kaband geophysical model function is valid for incidence angles of 30° to 50° at vertical transmit and receive polarization. Several particular cases of water-surface backscattering are presented by using this function.

*Keywords* – Scatterometer, Geophysical model function, Ka-Band, Sea Wind.

# I. INTRODUCTION

Many researchers have been investigating the microwave backscattering signatures of the water surface and solving the problem of remotely measuring wind over water during the last decades. A typical method for describing sea clutter is in the form of the normalized radar cross section (NRCS), the statistical distribution of the NRCS, the amplitude correlation and the spectral shape of the Doppler returns [1].

Use of a scatterometer, radar designed for measuring the surface scattering characteristics allows for studying sea surface backscattering and to estimate the wind vector over water because the NRCS of the water surface depends on wind speed and direction. Based on experimental data and scattering theory, a significant number of empirical and theoretical backscatter models and algorithms for retrieval of near-surface wind vector over water from satellite and airplane have been proposed [2–14]. This field develops actively with improvements of current and appearance of new models [15–22].

The backscatter of radio waves from sea surface varies considerably according to the incidence angle [6]. Near nadir, there is a region of quasi-specular return with a maximum of NRCS that decreases when increasing the angle of incidence. Between incidence angles of about 20° and 70°, the NRCS falls smoothly in a so-called "plateau" region. For medium incidence angles, microwave radar backscatter is predominantly due to the presence of capillary-gravity wavelets, which are superimposed on large gravity waves of the sea surface.

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<sup>3</sup>Klaus Schünemann is with Hamburg University of Technology, Denickestraße 22, 21073 Hamburg, Germany, E-mail: schuenemann@tu-harburg.de Small-scale sea waves of a length of approximately one half the radar wavelength are in Bragg resonance with an incident electromagnetic wave. At incidence angles greater than about 70°, there is a "shadow" region in which the NRCS falls dramatically, due to the shadowing effect of waves which are close to the radar blocking waves farther away.

The wind blowing over the sea modifies the water-surface backscatter properties. These depend on both wind speed and direction. The wind speed U can be determined by a scatterometer because a stronger wind will produce a larger NRCS  $\sigma^{\circ}(U, \theta, \alpha)$  at a medium incidence angle  $\theta$ , and a smaller NRCS at a small (near nadir) incidence angle. Wind direction can also be inferred because the NRCS varies as a function of the azimuth angle  $\alpha$  relative to the up-wind direction [12].

To retrieve the wind vector from NRCS measurements, the relationship between NRCS and near-surface wind, called the "geophysical model function", must be known. Scatterometer experiments have shown that the NRCS model function for medium incidence angles at appropriate transmit and receive polarization (vertical or horizontal) can be presented in several various forms. One of the widely used forms for the geophysical model function is [12]

$$\sigma^{\circ}(U,\theta,\alpha) = A(U,\theta) + B(U,\theta) \cdot \cos \alpha + C(U,\theta) \cdot \cos(2\alpha), (1)$$

where  $A(U,\theta)$ ,  $B(U,\theta)$  and  $C(U,\theta)$  are the Fourier terms that depend on sea surface wind speed and incidence angle,  $A(U,\theta) = a_0(\theta) \cdot U^{\gamma_0(\theta)}, \qquad B(U,\theta) = a_1(\theta) \cdot U^{\gamma_1(\theta)},$ and  $C(U,\theta) = a_2(\theta) \cdot U^{\gamma_2(\theta)}; \quad a_0(\theta), \quad a_1(\theta), \quad a_2(\theta), \quad \gamma_0(\theta),$  $\gamma_1(\theta)$  and  $\gamma_2(\theta)$  are the coefficients depending on the incidence angle. The term  $A(U,\theta)$  equals the azimuthally averaged NRCS; the term  $B(U,\theta)$  embodies the upwinddownwind asymmetry; and the term  $C(U,\theta)$  represents the upwind-crosswind anisotropy. Detailed procedures to obtain the above terms from backscatter values in the up-wind, down-wind, and cross-wind directions have been reported in [23]. The coefficients  $a_0(\theta)$ ,  $a_1(\theta)$ ,  $a_2(\theta)$ ,  $\gamma_0(\theta)$ ,  $\gamma_1(\theta)$ and  $\gamma_2(\theta)$  are determined empirically for an appropriate geophysical model function by using airborne or satellite measurements and validating surface measurements in addition. The coefficients are tabulated or presented as functions of incidence angle [2, 5, 8, 24].

Technological progress has made it possible to use a Kaband technique for airborne and satellite remote sensing. The usage of such a high frequency allows for reduced dimensions of the instruments on board as well as for increased resolution and accuracy in the estimation of sea surface topography [25].

Thus, there is a growing interest in studying Ka-band water surface backscattering and in developing the geophysical model function for this band. The Ka-band backscatter from water surface has been studied by using NRCS data from several airborne and wind-wave tank scatterometer experiments [4, 15, 25–29].

In this connection, an improved Ka-band geophysical model function will be presented below.

# II. GEOPHYSICAL MODEL FUNCTION

A Ka-band geophysical model function of the form (1) for incidence angles of 30° to 50° at vertical transmit and receive polarization has been previously presented in [28]. That geophysical model function has been developed using another NRCS model function from [4] given, however, only for up-, down- and cross-wind directions. Under the model development, the original up-wind NRCS curve from [4] at an incidence angle of 30° has been corrected in accordance with the wind-wave tank results reported in [23]. The correction had to be done, because the down-wind NRCS values tended to exceed the up-wind NRCS values at lower wind speeds as well as the down-wind NRCS values tended to exceed the cross-wind NRCS values at higher wind speeds.

Unfortunately, the geophysical model function described in [28] has a disadvantage. It shows up as a trough with a subsequent increase of the curve at incidence angles of  $47^{\circ}$  to  $50^{\circ}$  for near cross-wind azimuths, especially at low wind speeds.

To eliminate this imperfection, the model of the form (1) given in [28] has been recalculated. The following new coefficients for the Ka-band geophysical model function for vertical transmit and receive polarization, incidence angles of  $30^{\circ}$  to  $50^{\circ}$  and wind speeds of 5 to 20 m/s have been obtained

$$a_{0}(\theta) = 0.006036 - 0.0002031 \cdot \theta + 0.00000168 \cdot \theta^{2},$$

$$a_{1}(\theta) = -0.007776 + 0.0004421 \cdot \theta - 0.000005692 \cdot \theta^{2},$$

$$a_{2}(\theta) = 0.001151 + 0.0000134 \cdot \theta - 0.000000689 \cdot \theta^{2},$$

$$\gamma_{0}(\theta) = 4.902 - 0.198 \cdot \theta + 0.0028 \cdot \theta^{2},$$

$$\gamma_{1}(\theta) = 13.618 - 0.631 \cdot \theta + 0.00753 \cdot \theta^{2},$$

$$\gamma_{2}(\theta) = 5.896 - 0.258 \cdot \theta + 0.00348 \cdot \theta^{2},$$
(2)

where  $\theta$  is the incidence angle in degrees.

Figs. 1-3 show NRCS curves of form (1) with coefficients (2) versus incidence angle at wind speeds of 5, 10, 15, and 20 m/s for azimuth angles of  $70^{\circ}$ ,  $90^{\circ}$ , and  $110^{\circ}$ , respectively, at vertical transmit and receive polarization. Fig. 4 gives an example of NRCS curves versus azimuth angle for incidence angle of  $40^{\circ}$  at wind speeds of 5, 10, 15, and 20 m/s, respectively.



Fig. 1. Ka-band NRCS versus incidence angle for azimuth angle of 70° at wind speeds of 5, 10, 15, and 20 m/s, respectively, at vertical transmit and receive polarization



Fig. 2. Ka-band NRCS versus incidence angle for azimuth angle of 90° at wind speeds of 5, 10, 15, and 20 m/s, respectively, at vertical transmit and receive polarization



Fig. 3. Ka-band NRCS versus incidence angle for azimuth angle of 110° at wind speeds of 5, 10, 15, and 20 m/s, respectively, at vertical transmit and receive polarization



Fig. 4. Ka-band NRCS versus azimuth angle for incidence angle of 40° at wind speeds of 5, 10, 15, and 20 m/s, respectively, at vertical transmit and receive polarization

Thus, the new coefficients obtained for the geophysical model function of form (1) have allowed to eliminate the disadvantage of the previously-developed backscatter model.

## III. CONCLUSION

The previously-developed Ka-band backscatter model for incidence angles of  $30^{\circ}$  to  $50^{\circ}$  at vertical transmit and receive polarization [28] has been improved by eliminating its disadvantage near to cross-wind azimuths at incidence angles of  $47^{\circ}$  to  $50^{\circ}$ .

The improved geophysical model function can be used for developing and testing the wind retrieval algorithms for Kaband remote sensing instruments.

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